

Robust utility maximization with unbounded random endowment

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Abstract. This paper studies the problem of robust utility maximization with random endowment. When the endowment is possibly unbounded, but satisfies certain integrability conditions, we first prove the fundamental duality relation between the utility maximization and the dual problem, and the existence of a solution to the dual problem. Then the existence of an optimal strategy in a certain choice of admissible class is discussed. As an application, we introduce a robust version of utility indifference prices.

Key words: hedging, defaultable claims, convex duality, Neyman–Pearson lemma, jump processes

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